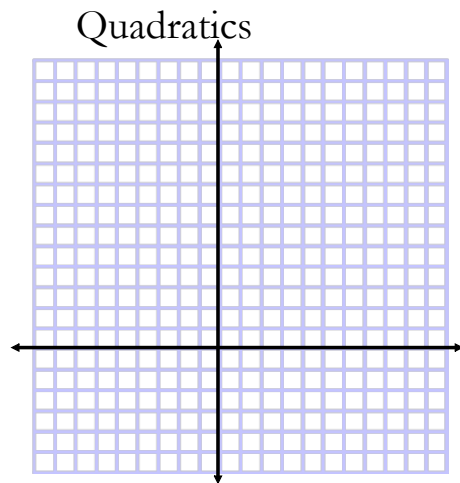


$$y = x^2$$

| x | y |
|-----|-----|
| -3 | |
| -2 | |
| -1 | |
| 0 | |
| 1 | |
| 2 | |
| 3 | |



Groups of 4:

For your equations:

- a) make a table of values
- b) plot the graph
- c) identify and label the:
 - i) vertex
 - ii) Axis of symmetry
 - iii) x- and y-intercepts

Group 1:

$$y = (x - 3)^2$$

$$y = (x + 5)^2$$

$$y = (x - 1)^2$$

Group 2:

$$y = x^2 - 3$$

$$y = x^2 + 2$$

$$y = x^2 + 1$$

Group 3:

$$y = 2x^2$$

$$y = \frac{1}{2}x^2$$

$$y = -3x^2$$

What is the effect of the following:

$$y = ax^2$$

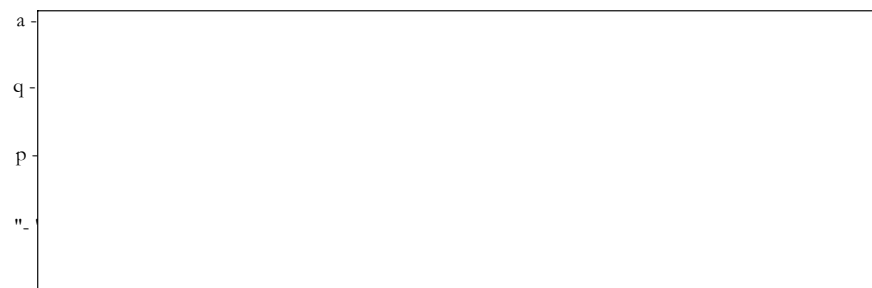
$$y = x^2 + k$$

$$y = (x - h)^2$$

$$y = -x^2$$

Transformations of Quadratics Functions

$$y = a(x - p)^2 + q \quad \text{vertex form}$$



Transformations of Quadratic Functions

RF3 - Analyze quadratic functions of the form $y = a(x - p)^2 + q$
 Determine the vertex, domain and range, direction of opening, axis of symmetry, x and y intercepts

1. Determine a rule for each transformation

A. $y = ax^2$

| | |
|-------------|-----------------------|
| $y = -x^2$ | $y = \frac{1}{2}x^2$ |
| $y = 2x^2$ | |
| $y = -2x^2$ | $y = -\frac{1}{2}x^2$ |

B. $y = x^2 + q$

| | |
|---------------|---------------|
| $y = x^2 + 4$ | $y = x^2 + 1$ |
| $y = x^2 - 3$ | $y = x^2 - 5$ |

C. $y = (x - p)^2$

| | |
|-----------------|-----------------|
| $y = (x - 3)^2$ | $y = (x + 4)^2$ |
| $y = (x + 1)^2$ | $y = (x - 2)^2$ |

3. Put it all together: $y = a(x - p)^2 + q$

Use your conclusions from #1 to state the vertex and the direction of opening for each function

| |
|-----------------------|
| $y = 2(x - 3)^2 + 4$ |
| $y = -3(x + 1)^2 - 5$ |

2. For each function: state the vertex, axis of symmetry and the maximum/minimum value

4. How many x-intercepts will each function have?

| | | |
|---------------------|----------------------|-------------------|
| $y = (x - 5)^2 - 7$ | $y = 2(x + 7)^2 + 3$ | $y = -3(x + 2)^2$ |
|---------------------|----------------------|-------------------|

5.

| Function | vertex | range | axis of symmetry | direction of opening | x int's? |
|-----------------------|--------|-------|------------------|----------------------|----------|
| $y = (x - 2)^2 + 3$ | | | | | |
| $y = -x^2 - 3$ | | | | | |
| $y = (x + 5)^2$ | | | | | |
| $y = -4(x + 1)^2 - 3$ | | | | | |

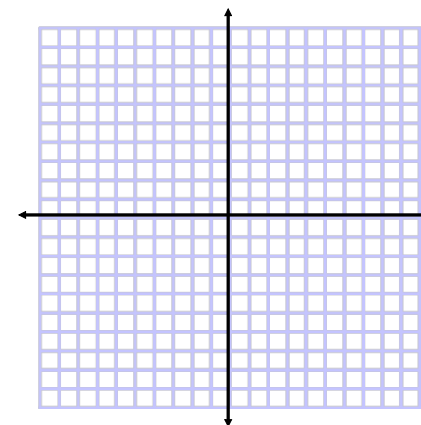
6. Use transformations to sketch each function

$y = (x + 3)^2 - 2$

$y = 2(x - 1)^2 + 3$

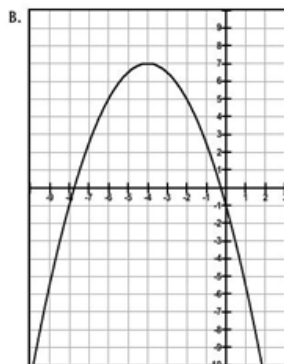
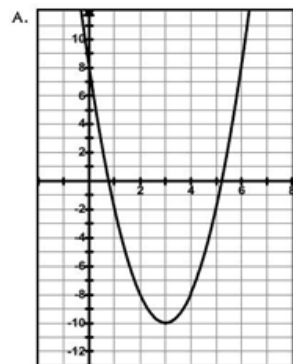
$y = -3(x + 2)^2 + 1$

$y = \frac{1}{2}(x + 4)^2$



Determining the equation of a quadratic equation.

EXAMPLE: Examine the following graphs and identify the equation of each function.



- | | |
|--|--|
| a. Identify the vertex. ⇨ _____ | a. Identify the vertex. ⇨ _____ |
| b. Identify the axis of symmetry. ⇨ _____ | b. Identify the axis of symmetry. ⇨ _____ |
| c. Identify the y-intercept. ⇨ _____ | c. Identify the y-intercept. ⇨ _____ |
| d. Identify the vertical stretch. ⇨ _____ | d. Identify the vertical stretch. ⇨ _____ |

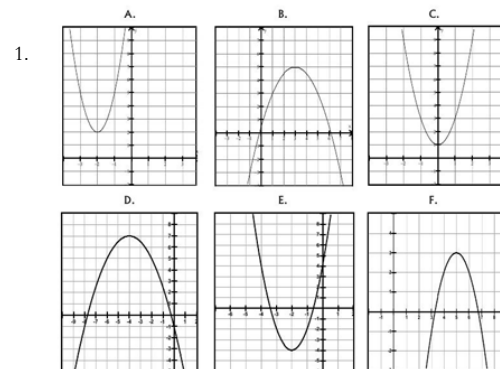
As you can see, using the characteristics of a quadratic function:

| | | |
|------------------|--------|--|
| Vertex | (p, q) | |
| Axis of Symmetry | x=p | We can write the equation in vertex form |
| Vertical Stretch | a | $y = a(x - p)^2 + q$ |

The most challenging characteristic to find is the vertical stretch. This value can be determined if we know the vertex and one other point.

A golf ball is hit from the fairway with a high chip shot. It reaches a maximum height of 20 m and lands on the green 10 m away. Determine the equation that describes the golf ball's path.

Write the equation of the following in vertex form:



- vertex (2, 5) and has a y-intercept of 3
 - vertex (6, -2) and has a y-intercept of -8
 - vertex (4, 3) and has x-intercepts 2 and 6
 - vertex (-2, -4) and has x-intercepts -4 and 0
- Find the vertical stretch and write the equation in vertex form.

- A rock is thrown into the air from an initial height of 2 metres. After 2 seconds it reaches a maximum height of 10 metres. Determine the equation of the quadratic function that describes the path of the rock.
- A wedding arch is in the shape of a parabola. If the arch is 2 m wide and 3 m tall, determine the equation that describes the shape of the arch.
- An arrow is fired into the air and reaches a maximum height of 30 m at a horizontal distance of 50 m from where it is fired. It sticks in the ground 90 m away from where it is fired.
 - determine the equation of the quadratic function that describes the path of the arrow.
 - How high is the arrow after travelling a horizontal distance of 80 m?
- A football is kicked for a field goal attempt and it reaches a maximum height of 25 m at a horizontal distance of 20 m.
 - Determine the equation of the quadratic function that describes the path of the football.
 - If the field goal marker is 35 m away at a height of 3 m, would the kick score the points?

1. Quadratics.notebook

March 18, 2016

RF4. Analyze quadratic functions of the form to identify characteristics of the corresponding graph, including: vertex, domain and range, direction of opening, axis of symmetry, x- and y-intercepts; and to solve problems. [CN, PS, R, T, V]

Vertex form: $y = (x - 2)^2 + 7$

Expanded:

Standard Form:

Going backwards, we need to use a process called completing the square to return (or to convert) to vertex form

$$y = x^2 - 4x + 11$$

we need to make $y = x^2 - 4x + \underline{\hspace{1cm}}$ part of a perfect square trinomial

$$y = x^2 - 5x + 1$$

More completing the square!

$$y = -x^2 + 6x + 7$$

When $a \neq 1$, you need to group the first two terms and factor the leading coefficient out.

$$y = x^2 + 6x + 5$$

$$y = x^2 - 10x + 12$$

$$y = 3x^2 + 12x - 5$$

Using completing the square to derive the quadratic formula:

$$y = ax^2 + bx + c$$

2. Complete the square and find the vertex!

$$y = -x^2 - 6x + 2$$

$$y = x^2 + 5x - 2$$

Complete the square to write in vertex form

1. $y = x^2 + 16x - 2$

2. $y = x^2 - 7x - 5$

SCO: RF5. Solve problems that involve quadratic equations. [C, CN, PS, R, T, V]

Solving a Quadratic Equation

| | | |
|----------------|---------------|--------------|
| Roots | zeros | x-intercepts |
| of an equation | of a function | of a graph |

★ These all mean to let $y=0$ and solve for x

Methods used to solve quadratic equations

1. Square root
 $x^2 - 49 = 0$

2. Factor
 $x^2 + 3x - 10 = 0$

3. $y = -x^2 - 14x + 3$

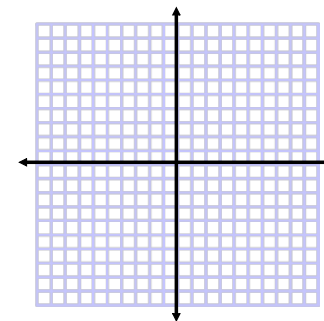
4. $y = 4x^2 - 12x + 7$

3. Complete the square
 $x^2 - 6x + 1 = 0$

4. Quadratic formula
 $x^2 - 6x + 1 = 0$

5. $y = -3x^2 + 18x + 1$

5. Graph
 $(x - 2)^2 - 4 = 0$
 $x^2 - 4x = 0$



Show that the following quadratic equations are equivalent

standard form

vertex form

$$y = x^2 + 10x + 7$$

$$y = (x + 5)^2 - 18$$

A Quadratic Equation has two roots

standard form

vertex form

factored form

$$y = ax^2 + bx + c$$

$$y = a(x - p)^2 + q$$

$$y = a(x - r)(x - s)$$

What kind of roots will a quadratic function have?

$$y = (x + 2)^2 - 5$$

$$y = (x - 3)^2$$

$$y = (x - 1)^2 + 3$$

How do you determine the number of roots when in standard form?

$$y = x^2 + 4x - 1$$

$$y = x^2 - 6x + 9$$

$$y = x^2 - 2x + 5$$

The Discriminant tells you what type of roots the quadratic function will have



if $D > 0$

if $D = 0$

if $D < 0$

$$y = x^2 + 4x + 2$$

$$y = x^2 - 10x + 25$$

$$y = x^2 + 2x + 5$$